

# Challenges in Bayesian Network Modelling of Climate and Weather Data

---

Marco Scutari  
[scutari@idsia.ch](mailto:scutari@idsia.ch)

Dalle Molle Institute for  
Artificial Intelligence

November 6, 2019

## Natural Systems are Complex Systems

---

Natural phenomena can only be modelled as **complex systems** in which

- there are many components that interact with each other;
- their interplay produces non-obvious behaviour;
- they develop over time and space in response to the surrounding environment.

Two scientific research fields in which this has increasingly become apparent are **environmental sciences** and **biological sciences** (genetics, systems biology, etc.).

Classic statistical models that focus on explaining or predicting a single component of such phenomena often fail to capture the big picture. **Network models**, on the other hand, focus on capturing the **interplay between components from a systems perspective**, without necessarily restricting their attention to a single one.

## Bayesian Networks as a Model for Complex Systems

---

**Bayesian networks** (BNs) [9] implement this systems approach with:

- a **network structure**, a directed acyclic graph in which each node corresponds to a random variable  $X_i$ ;
- a global probability distribution  $P(\mathbf{X})$  with parameters  $\Theta$ , which can be factorised into smaller **local probability distributions** according to the arcs present in the graph.

The main role of the network structure is to express the **conditional independence** relationships among the variables in the model through **graphical separation**, thus specifying the factorisation of the global distribution:

$$P(\mathbf{X}) = \prod_{i=1}^N P(X_i \mid \Pi_{X_i}; \Theta_{X_i}) \quad \text{where} \quad \Pi_{X_i} = \{\text{parents of } X_i\}.$$

## Why Use Bayesian Networks?

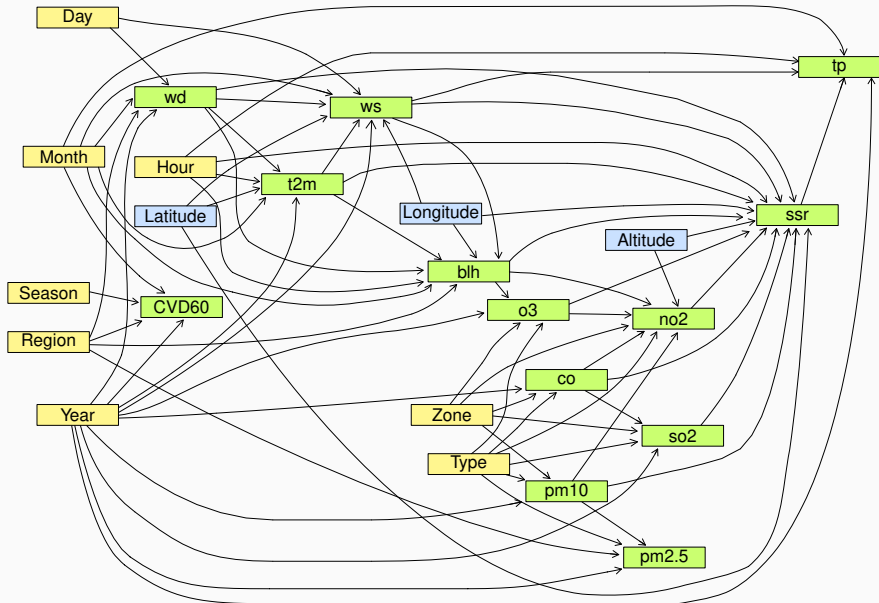
---

Four main reasons:

- Both the network structure and the parameters can be **learned efficiently** from data [18]; and available **prior information can be incorporated** in the learning process as well [2, 13, 4].
- The network structure provides a **high-level qualitative view** of the phenomenon that can easily be used by non-statisticians.
- **Automated reasoning** can quantify the probability of any event of interest given available evidence using standard algorithms.
- With some additional assumptions BNs can be interpreted as **causal models** [14].

Several **applications in environmental sciences**: studying species dynamics [1, 19]; the impact of climate change on groundwater [12]; how to best manage water reservoirs under infrequent rainfalls [15]; the effects of El Niño [17]; and the impact of pollution [20].

# Modelling Air Pollution, Climate and Health Data



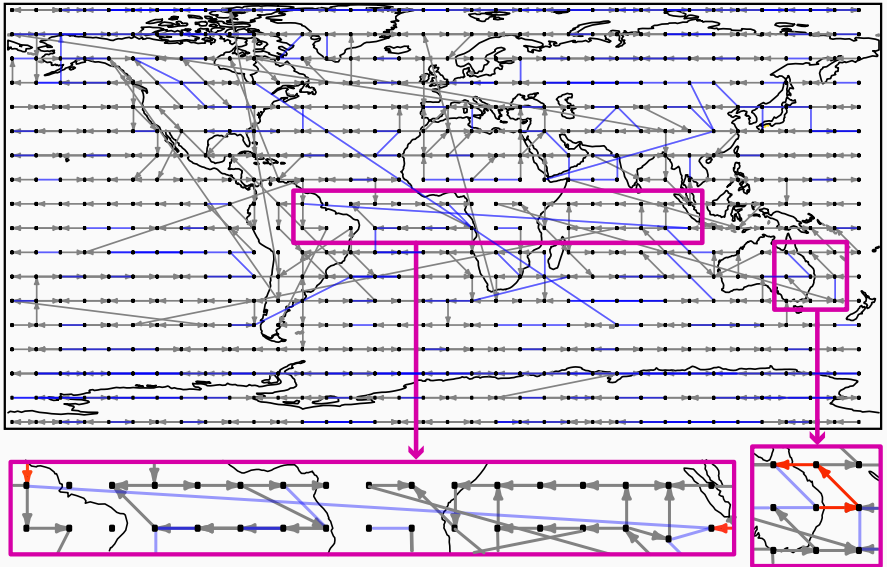
## Modelling Air Pollution, Climate and Health Data

---

C. Vitolo, M. Scutari, M. Ghalaieny, A. Tucker and A. Russell (2018). “Modeling Air Pollution, Climate, and Health Data Using Bayesian Networks: A Case Study of the English Regions.” *Earth and Space Science*, 5(4), 76–88. [20]

- Almost **50 million records** spanning the period 1981–2014.
- 24 features: various **air pollutants** (O<sub>3</sub>, PM<sub>2.5</sub>, PM<sub>10</sub>, SO<sub>2</sub>, NO<sub>2</sub>, CO) measured in 162 monitoring stations, their **geographical characteristics** (latitude, longitude, latitude, region and zone type), weather (wind speed and direction, temperature, rainfall, solar radiation, boundary layer height), **demography** and **mortality rates**.
- The model **represents known processes in atmospheric chemistry with a good degree of accuracy**.

# Climate Data Analysis



M. Scutari, C. E. Graafland and J. M. Gutiérrez (2019). “Who Learns Better Bayesian Network Structures: Accuracy and Speed of Structure Learning Algorithms.” *International Journal of Approximate Reasoning*, 115:235–253. [17]

- **Monthly surface temperature values** on a global  $10^\circ$ -resolution regular grid from 1981 to 2010.
- Local dependencies are strong since they are the result of the short-term evolution of atmospheric thermodynamic processes. Distant **teleconnected dependencies** resulting from large-scale atmospheric oscillation patterns are in general weaker, but they are key for understanding regional climate variability.
- Altered **probabilities of high temperatures** in the Indian Ocean when El Niño-like evidence is introduced in the BN.



## Assumptions and Limitations of Bayesian Networks

---

Two assumptions that are typically made in BN learning are particularly problematic:

- **Complete Data**: the data contain no missing values.
- **Independent Observations**: observations are jointly independent of each other.

Other common assumptions that may be problematic:

- Categorical variables are **multinomial**, continuous variables are **Gaussian** or **mixtures of Gaussians**.
- The network is **sparse**, with a number of arcs comparable to the number of nodes.

The computational complexity of learning can also be an issue: linear in the sample size but **quadratic** in the number of variables (and that is assuming the network is sparse).

## Learning from Incomplete Data

---

We can learn the network structure from incomplete data using a variation of the EM algorithm called **Structural EM** [5, 6]:

- in the **E**-step, we complete the data by computing the expected sufficient statistics using the current network structure;
- in the **M**-step, we find the structure that maximises the expected likelihood or posterior probability for the completed data.

The parameters can be learned with the classic EM [10].

However:

- The Structural EM is extremely **computationally intensive**; the shortcuts used in practical implementations void its theoretical guarantees.
- There is **no literature** on this for continuous or hybrid data, only for categorical data.
- Data are assumed to be **missing (completely) at random**.

## Take the Spatio-Temporal Structure of the Data into Account

---

For instance, the local distribution of a Gaussian variable with continuous parents is assumed to be

$$X_i = \mu_{X_i} + \Pi_{X_i} \beta_{X_i} + \varepsilon_{X_i}, \quad \varepsilon_{X_i} \sim N(0, \Sigma_{X_i}), \quad \Sigma_{X_i} = \sigma_{X_i}^2 \mathbf{I}_n;$$

all the parameter estimators and goodness-of-fit scores are borrowed from classic linear regression.

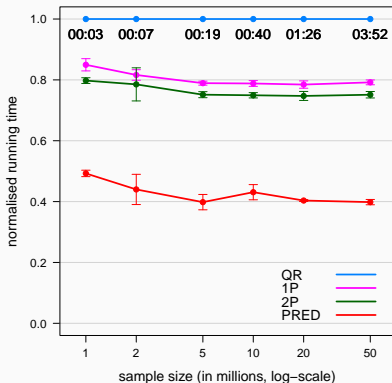
The logical solution would be to use an **appropriate covariance structure** [3] such as an isotropic exponential structure

$$\Sigma_{X_i} = [\sigma_{jk}] \quad \sigma_{jk} = \sigma^2 \exp\{-d_{jk}/\theta\}$$

instead of  $\sigma_{jk} = 0$  for all  $j \neq k$ . It comes at a cost in terms of speed, but it is **feasible unlike the MCMC approaches** for state space models such as [7].

## Improve Computational Efficiency

- Many algorithms display embarrassing or coarse-grained **parallelism** [16].
- There are many approaches in statistical genetics that **optimise sequential linear model evaluation** [11], including for correlated observations.
- For discrete data, there are **efficient data structures** that can be leveraged [8].



(Classic **closed-form results** can help too [18]!)

## Conclusions and Remarks

---

- BNs are naturally suited to modelling **complex systems** as networks.
- BNs have several key advantages: they can incorporate **prior information** while learning them from data; they are **easy to interpret** for non-statisticians; and they allow **automated and causal reasoning**.
- Their fundamental assumptions must be weakened to improve their usability in environmental sciences, to **handle incomplete and spatio-temporal data effectively**.
- **Computational complexity** is also an issue, but there is literature to draw from for inspiration.

## Acknowledgements

---



Catharina Elisabeth Graafland  
José Manuel Gutiérrez  
*Institute of Physics of Cantabria (CSIC-UC)*



Allan Tucker  
Andrew Russell  
Mohamed Ghalaieny  
*Brunel University London*



Claudia Vitolo  
*European Centre for Medium-Range  
Weather Forecasts*

Thanks!

# References I

---



A. Aderhold, D. Husmeier, J. J. Lennon, C. M. Beale, and V. A. Smith.  
Hierarchical Bayesian Models in Ecology: Reconstructing Species Interaction Networks from Non-Homogeneous Species Abundance Data.  
*Ecological Informatics*, 11:55–64, 2012.



R. Castelo and A. Siebes.  
Priors on Network Structures. Biasing the Search for Bayesian Networks.  
*International Journal of Approximate Reasoning*, 24(1):39–57, 2000.



P. J. Diggle, P. Heagerty, K.-Y. Liang, and S. L. Zeger.  
*Analysis of Longitudinal Data*.  
Oxford University Press, 2nd edition, 2013.



M. J. Druzdzel and L. C. van der Gaag.  
Elicitation of Probabilities for Belief Networks: Combining Qualitative and Quantitative Information.  
*In Proceedings of the 11th Conference on Uncertainty in Artificial Intelligence*, pages 141–148, 1995.



N. Friedman.  
Learning Belief Networks in the Presence of Missing Values and Hidden Variables.  
*In Proceedings of the 14th International Conference on Machine Learning*, pages 125–133, 1997.



## References II

---



**N. Friedman.**

**The Bayesian Structural EM Algorithm.**

*In Proceedings of the Fourteenth Conference on Uncertainty in Artificial Intelligence*, pages 129–138, 1998.



**I. D. Jonsen, R. A. Myers, and J. M. Flemming.**

**Meta-Analysis of Animal Movement Using State-Space Models.**

*Ecology*, 84(11):3055–3063, 2003.



**S. Karan, M. Eichhorn, B. Hurlburt, G. Iraci, and J. Zola.**

**Fast Counting in Machine Learning Applications.**

*In Proceedings of the 34th Conference on Uncertainty in Artificial Intelligence*, pages 540–549, 2018.



**D. Koller and N. Friedman.**

***Probabilistic Graphical Models: Principles and Techniques.***

MIT Press, 2009.



**S. L. Lauritzen.**

**The EM Algorithm for Graphical Association Models with Missing Data.**

*Computational Statistics and Data Analysis*, 19(2):191–201, 1995.



**C. Lippert, J. Listgarten, Y. Liu, C. M. Cadie, R. I. Davidson, and D. Heckerman.**

**FaST Linear Mixed Models for Genome-Wide Association Studies.**

*Nature Methods*, 8(10):833–837, 2011.

## References III

---



J.-L. Molina, D. Pulido-Velázquez, J. L. García-Aróstegui, and M. Pulido-Velázquez.  
Dynamic Bayesian Networks as a Decision Support Tool for Assessing Climate Change Impacts on Highly Stressed Groundwater Systems.  
*Journal of Hydrology*, 479:113–129, 2013.



S. Mukherjee and T. P. Speed.  
Network Inference Using Informative Priors.  
*Proceedings of the National Academy of Sciences*, 105(38):14313–14318, 2008.



J. Pearl and D. Mackenzie.  
*The Book of Why: the New Science of Cause and Effect*.  
Basic Books, 2018.



R. F. Ropero, M. J. Flores, R. Rumí, and P. A. Aguilera.  
Applications of Hybrid Dynamic Bayesian Networks to Water Reservoir Management.  
*Environmetrics*, 28:e2432, 2017.



M. Scutari.  
Bayesian Network Constraint-Based Structure Learning Algorithms: Parallel and Optimised Implementations in the bnlearn R Package.  
*Journal of Statistical Software*, 77(2):1–20, 2017.

## References IV

---



M. Scutari, C. E. Graafland, and J. M. Gutiérrez.

Who Learns Better Bayesian Network Structures: Accuracy and Speed of Structure Learning Algorithms.

*International Journal of Approximate Reasoning*, 115:235–253, 2019.



M. Scutari, C. Vitolo, and A. Tucker.

Learning Bayesian Networks from Big Data with Greedy Search: Computational Complexity and Efficient Implementation.

*Statistics and Computing*, 25(9):1095–1108, 2019.



N. Trifonova, A. Kenny, D. Maxwell, D. Duplisea, J. Fernandes, and A. Tucker.

Spatio-Temporal Bayesian Network Models with Latent Variables for Revealing Trophic Dynamics and Functional Networks in Fisheries Ecology.

*Ecological Informatics*, 30:142–158, 2015.



C. Vitolo, M. Scutari, A. Tucker, and A. Russell.

Modelling Air Pollution, Climate and Health Data Using Bayesian Networks: a Case Study of the English Regions.

*Earth and Space Science*, 5(4):76–88, 2018.